

Motivating Smartphone Collaboration in Data Acquisition and Distributed Computing

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Abstract—This paper analyzes and compares different incentive mechanisms for a master to motivate the collaboration of smartphone users on both *data acquisition* and *distributed computing* applications. To collect massive sensitive data from users, we propose a reward-based collaboration mechanism, where the master announces a total reward to be shared among collaborators, and the collaboration is successful if there are enough users wanting to collaborate. We show that if the master knows the users' collaboration costs, then he can choose to involve only users with the lowest costs. However, without knowing users' private information, then he needs to offer a larger total reward to attract enough collaborators. Users will benefit from knowing their costs before the data acquisition. Perhaps surprisingly, the master may benefit as the variance of users' cost distribution increases. To utilize smartphones' computation resources to solve complex computing problems, we study how the master can design an optimal contract by specifying different task-reward combinations for different user types. Under complete information, we show that the master involves a user type as long as the master's preference characteristic outweighs that type's unit cost. All collaborators achieve a zero payoff in this case. If the master does not know users' private cost information, however, he will conservatively target at a smaller group of users with small costs, and has to give most benefits to the collaborators.

Index Terms—Smartphone application, data acquisition, distributed computing, game theory, contract theory

1 INTRODUCTION

SMARTPHONES are becoming the mainstream in mobile phones. According to a ComScore survey in 2010, over 45.5 million people owned smartphones out of 234 million total mobile phone subscribers in the United States [2]. In 2012, the global smartphone shipments grew 43 percent annually by reaching a record 700 million units [3].

Given millions of smartphones sold annually, recent phone applications start to utilize the power of smartphone users' collaborations [4], [5]. In such an application, there is a *master* (e.g., Apple or Google in the following examples) who wants to implement some application or service based on user collaborations. We can categorize these applications in two types as follows.

In the first type of *data acquisition* application, a master wants to acquire enough data from smartphone users to build up a database. According to [5], Apple's iPhone and Google's Android smartphones regularly transmit their owners' location data (including GPS coordinates) back to Apple and Google without users' agreements, respectively. For example, an Android phone collects its

location data every few seconds and transmits the data to Google at least several times an hour. The phone also transmits back the name, location, and signal strength of any nearby Wi-Fi networks. After collecting enough location data from users, Google can successfully build a massive database capable of providing location-based services (LBSs). One service can be live map of auto traffics, where the dynamics of users' location data on a highway indicate whether there is a traffic jam. Another service can be constructing a large-scale public Wi-Fi map. According to [6], the global location-based service market is growing strongly, and its revenue is expected to increase from US \$2.8 billions to US\$10.3 billions between 2010 and 2015. In order to perform the above data acquisition, a lot of efforts need to be spent to get users' consent and protect users' privacy (e.g., [7], [8], [9]). When a user collaborates in this kind of applications, he will incur a cost such as loss of privacy.

In the second type of *distributed computing* application, a master wants to solve complex engineering or commercial problems inexpensively using distributed computation power. Smartphones now have powerful and power-efficient processors (e.g., Dual-core A6 chip of Apple iPhone 5 which is comparable to many laptops' CPUs several years ago), outstanding battery life, abundant memory, and open operating systems (e.g., Google Android) [10] that make them suitable for complex processing tasks. Since millions of smartphones remain unused most of the time, a master might want to solicit smartphone collaborations in distributed computing (e.g., [11], [12], [13]). In this case, a user's collaboration cost may be due to loss of energy and reduction of physical storage.

In this paper, we will design incentive mechanism for smartphone collaborations in data acquisition and

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distributed computing applications, both of which aim to incentivize users to participate the collaboration through proper rewards. Then we can compare the similarity and difference in mechanism design for both applications. For each type of applications, we will similarly consider various information scenarios, depending on what the master and users know. In particular, the master may or may not know each smartphone user's characteristics such as collaboration costs and collaboration efficiencies.

The two types of applications have different requirements and lead to different models. Collaborators in data acquisition usually take similar tasks and hence should be rewarded similarly, whereas collaborators in distributed computing will undertake different amounts of work according to their different computation capabilities. More specifically, in data acquisition applications, we consider a threshold-based revenue model, where a master can earn a fixed positive revenue only if he can involve enough (larger than a threshold) smartphone users as collaborators, such that he can build a large enough database to support the application like the live map of auto traffics. Since data acquisition only requires simple periodic data reporting, we can assume that users are homogeneous in contribution and efficiency.¹ In distributed computing applications, however, we consider a model where the master's revenue increases in users' efforts. Also, users are heterogeneous in computing efficiencies and should be treated differently. For example, the most efficient users should be highly rewarded to encourage them to undertake large tasks.

Our key results and contributions are as follows:

- *New reward-based mechanism to motivate data acquisition:* We propose a Stackelberg game model under incomplete information that captures interactions between the master and users in Section 2. The master first announces the total reward to be allocated among collaborators. To decide to join or not, each user then estimates other users' decisions in predicting the chance of collaboration success and his expected reward. We show that it is better to reward users' collaboration efforts regardless the result of the collaboration. This encourages users to collaborate, and hence increases the chance of collaboration success.
- *Performance of reward-based mechanism:* Under complete or symmetrically incomplete information, the master can decide a small reward to attract enough users. But if users know their costs while the master does not (asymmetrically incomplete information), the master has to offer a large total reward to guarantee enough collaborators, and users benefit from holding private information. Perhaps surprisingly, when the master does not need a large number of collaborators, he can

benefit as the variance of users' cost distribution increases.

- *New contract-based mechanism to motivate distributed computing:* In Section 3, we use contract theory to study how a master efficiently decides different task-reward combinations for heterogeneous users. By satisfying individual rationality and incentive compatibility, our contract enables all users to truthfully reveal their private information and maximizes the master's utility.
- *Performance of contract-based mechanism:* Under complete information, the master involves a user type as long as the master's preference of the type is larger than the user cost. All collaborators get a zero payoff. But if users can hold their private information from the master, the master will conservatively target at a smaller group of efficient users with small costs. He has to give most benefits to the collaborators and a collaborator's payoff increases in the computing efficiency.

Most proofs for this paper in Appendices are removed to another separate supplemental file, according to TMC new requirement. These appendices can also be found in our online technical report [37].

1.1 Related Work

Our first collaboration model on data acquisition is closely related to the literature on location-based services [14]. In LBS, a customer needs to report his current location to the database server in order to receive his desired service. Prior work are focusing on how to manage data and how customers can safely communicate with the database server (e.g., [8], [9], [15]), especially when the massive database has already been built up. Other work considered the technical issues of data collection from users [15]. Our paper focuses on the master's problem of incentive mechanism design for attracting enough users (larger than some threshold) using reward to provide location data, so that the master can build a LBS later on. Only recently people started to look at users' incentives to reveal information. For example, Yang et al. [16] also designed incentive mechanisms for involving sensors. The model in [16] does not involve the issue of collaboration cost estimation and collaboration success probability, and the main results were mainly derived through simulations. Actually, most Stackelberg game models assume complete information yet this paper focuses on incomplete information.

Our second collaboration model is relevant to mobile grid computing, which integrates mobile wireless devices into grid computing (e.g., [17], [18], [19]). The main focus of mobile grid computing literature is on the technical issues of resource management or load balancing (e.g., [18], [19]). Only few results have considered (mobile) users' incentives issues in joining in collaboration [20], [21], [22]. Kwok et al. in [21] evaluate the impact of selfish behaviors of individual users in a Grid. Subrata et al. in [22] present a Nash bargaining solution for load balancing among multiple masters. Sim in [20] use a two-player alternating bargaining model to study collaboration

1. For example, a huge number users take the same simple task by periodically reporting their GPS location data, and it is reasonable and fair for the master to reward them equally (as in Amazon Mechanical Turk). It is difficult for the master to differentiate contributions and rewards to a huge number of users, and monitoring and updating his beliefs of users' private information is often impractical.

between masters and users. The novelty of our model is that a master interacts with all users simultaneously to distribute computing work, and users are heterogeneous in their computing efficiencies and costs. We propose a new contract-based mechanism that maximizes the master's profit.² Unlike our first collaboration model using a total reward to incentivize the same periodic data acquisition, here this contract mechanism aims to assign *different* amounts of work to different user types, and does not require a threshold-based collaboration success.

2 COLLABORATIONS ON DATA ACQUISITION

2.1 System Model of Data Acquisition

In this application, the master is interested in building up a database by collecting information from enough smartphone users. We consider a set $\mathcal{N} = \{1, \dots, N\}$ of smartphones, and the total number N is publicly known.³ User $i \in \mathcal{N}$ has a collaboration cost $C_i(p_i, e_i) > 0$, which is generally a function (e.g., weighted sum) of his privacy loss p_i and energy consumption e_i illustrated as follows:

- *Privacy loss p_i* : By reporting sensitive data (e.g., GPS location coordinates), a user's loss can be psychological worry of losing privacy, discomfort due to frequent annoyance from unwanted advertising in location-based services, or even property loss due to disclosure of bank account information in data reporting (e.g., [25], [26], [27]).
- *Energy consumption e_i* : Collecting and transmitting data periodically to the master's data center consumes a user's smartphone battery. According to [28] and [29], the consumed energy depends on the details of the data acquisition task, including the interaction efficiency among various layers (e.g., radio channel state, transport layer, application layer, and user interaction layer). The measurement data (e.g., radio power) for some typical applications and platforms can be found in [28] and [29].

We assume that the distributions of users' privacy losses and energy consumptions are independent. As combinations of the two terms, we assume that the collaboration costs are independently and identically distributed, with a mean μ and a cumulative probability distribution function $F(\cdot)$.⁴ We do not impose any further assumptions on the properties of the distribution $F(\cdot)$ in this paper.

We consider a *threshold revenue model* for the master. If the master attracts at least n_0 users as collaborators, he will successfully build the database and receive a revenue of V . Otherwise, the master does not receive any revenue. Such a

2. Our designed contract-based mechanism here belongs to screening contract category [23] and is similar to that in our previous work [24] in methodology, but that work focuses on a different problem on cooperative spectrum sharing and the derived mechanisms as well as results are significantly different.

3. We assume all N users are active. The master (e.g., Apple) learns the number of active users (e.g., iPhones) by checking users' usage history, or send users control messages for status confirmation.

4. This assumption makes our analysis tractable to deliver clean engineering insights. Yet our results can be extended to the case where the costs are not identically distributed. Then, for example, a user with a larger mean value of cost distribution is less willing to collaborate.

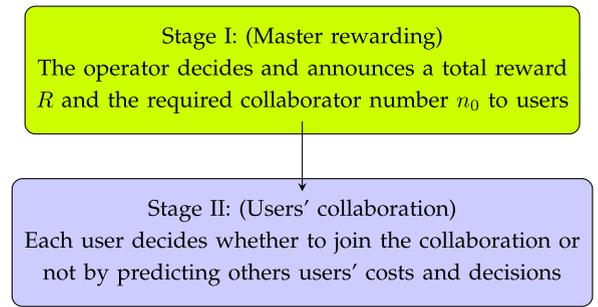


Fig. 1. Stackelberg game between the master and users.

threshold model has many practical applications. In the example of collecting GPS data to establish a live map of auto traffics, several users' movement information along the same highway will be enough to tell whether the highway is congested or not.

As shown in Fig. 1, the master interacts with the users through a two-stage process. In Stage I, the master announces (R, n_0) , where R is the total reward to all users and n_0 is the threshold number of required collaborators. In Stage II, each user chooses to be a collaborator or not.⁵ Similar to Amazon Mechanical Turk,⁶ the master here sets up a database with users' account and payment information and can automatically pay each involved user. A user's received reward can be monetary return or some promotion to use the relevant location-based service afterwards.

We want to mention that our model is also applicable to the scenario where users do not join the collaboration simultaneously. As long as users submit their "sealed" responses to the master's collaboration invitation and cannot check others' behaviors, our results will remain valid. On the other hand, if a user learns from others' behaviors to determine the current number of committed users, then the analysis of such a dynamic decision evolution becomes very challenging. Some methods about social learning and mean field approximation may be used in the scenario (though clean theoretical results are still hard to obtain) [30], [31].

Assume that there are n out of N users willing to serve as collaborators in Stage II. There are two models for a collaborator's payoff:

- *Model (A) (Reward for collaboration effort)*: A collaborator i 's payoff is

$$\left(\frac{R}{n} - C_i\right) \mathbf{1}_{\{n \geq n_0\}}, \quad (1)$$

where $\mathbf{1}_{\{X\}}$ is the indicator function (equals 1 when event X is true). That is, if the collaboration is successful, user i pays his collaboration cost C_i , and

5. To support some real-time location-based services (e.g., maps of live traffic information), we require users' quick responses in order to update the database. Such a quick collection of data is feasible now (e.g., like invitation messaging to reveal location in many iPhone apps). Amazon Mechanical Turk also supports online interaction between masters and users. Some media masters like Google may also have urgent needs to report some critical events by asking users in a certain area to upload photos and videos.

6. See the Amazon link <https://www.mturk.com/mturk/welcome>.

gets the reward R/n (equally and fairly shared among n collaborators since they undertake the same task in fixed and periodic data reporting). We can also view R/n as in a *lottery* scenario where each collaborator having equal probability $1/n$ to win the total reward R . In this case, n users will only collaborate if the master notifies them that $n \geq n_0$ and the collaboration will be successful. This means that no users will pay collaboration cost if the collaboration is not successful. Here, we assume that the master will truthfully inform the collaborators about the value of n .⁷

- *Model (B) (Reward only with successful collaboration):* A collaborator i receives a payoff

$$\frac{R}{n} \mathbf{1}_{\{n \geq n_0\}} - C_i. \quad (2)$$

That is, collaborator i always pays his collaboration cost C_i , and will get the reward R/n only if the collaboration is successful. This model considers that collaborators will contribute before they know the value of n (which will be announced to them by the master after data acquisition).

In both model, the master obtains a profit of

$$(V - R) \mathbf{1}_{\{n \geq n_0\}}.$$

For illustration purpose, we now only focus on Model (A) in this section. The discussion of Model (B) can be found in Appendix F, which can be found on the Computer Society Digital Library at <http://doi.ieeecomputersociety.org/10.1109/TMC.2014.2307327>. It should be noted that users under Model (A) are more willing to collaborate than under Model (B), which is not surprising since they face a lower risk in Model (A). The master also prefers Model (A) to Model (B) since he needs to compensate lower risk and fewer cost to motivate users' collaboration.

The *collaboration game* is a two-stage Stackelberg game, and we would like to characterize the subgame perfect equilibrium (SPE) that specifies players' stable choices in all stages [32]. The way to analyze Stackelberg game is backward induction. The master in Stage I and users in Stage II are risk-neutral and want to maximize their own payoffs, respectively. We will first analyze Stage II, where the users play a game among themselves based on the value of the reward R and the threshold n_0 .⁸ Users reach a *Nash equilibrium* (NE) in this stage, if no user can improve his payoff by changing his strategy (collaborate or not) unilaterally. The Nash equilibrium in Stage II leads to a collaboration success probability $P(n \geq n_0|R)$. As we will see, there may be multiple Nash equilibria in Stage II. Then we study Stage I, where the master chooses the value of R to maximize his expected profit

$(V - R)P(n \geq n_0|R)$. These two-step analysis enables us to obtain an SPE of the whole two-stage game.

Next we will analyze the Stackelberg game, and study how the master's and the users' information about the collaboration costs will affect the outcome.

2.2 Collaboration under Complete Information

We first consider the complete information scenario, where the master and all users know the cost C_i of every user $i \in \mathcal{N}$. This is possible only in some special cases where the master and users have extensive prior collaboration experiences. The main reason for studying this model is to provide a performance benchmark for later discussions of more realistic incomplete information scenarios.

We assume that no two users have the exactly same cost. Our results also apply to the case of homogeneous users, where we can randomly break the tie among homogeneous users at the boundary. This will lead to more than one equilibrium. Without loss of generality, we reorder the users' costs in ascending order, i.e., $C_1 < C_2 < \dots < C_N$ and C_{n_0} is the n_0 th smallest cost. The equilibrium of the collaboration game is as follows.

Theorem 1 (Collaboration Under Complete Information).

Recall that C_{n_0} is the n_0 th smallest collaboration cost among all N users. The collaboration game admits the following unique pure strategy SPE:

- If $V < n_0 C_{n_0}$, then the master does not want to initiate the collaboration in Stage I and sets $R^* = 0$. No user will become collaborator in Stage II.
- If $V \geq n_0 C_{n_0}$, the master offers a reward $R^* = n_0 C_{n_0}$ in Stage I. In Stage II, every user i with $C_i \leq C_{n_0}$ collaborates and obtains a nonnegative payoff $C_{n_0} - C_i$, and the remaining $N - n_0$ users decline to collaborate and get a zero payoff. The profit of the master is $V - n_0 C_{n_0}$.

The proof of Theorem 1 is given in Appendix A, available in the online supplemental material.

We can show that users will not benefit from using a mixed-strategy. But this may not be the case with symmetrically incomplete information.

2.3 Collaboration under Symmetrically Incomplete Information

Now we consider the symmetrically incomplete information scenario, where both the master and the users only know the cumulative probability distribution function $F(\cdot)$ of the collaboration costs with the mean μ .⁹ A user i even does not know the precise value of his own cost C_i .¹⁰ In this case, we can view all users as homogeneous.

7. In reality, the master may cheat users by announcing a larger value of n , then he can give less reward to each actual collaborator. But there are some approaches to prevent this. For example, there could be a third party to monitor how many collaborators are finally involved and punish the master if cheating is detected.

8. We consider that each user will join the collaboration as long as his payoff is nonnegative. Yet our results can still be generalized to the case where users have positive reserve payoffs.

9. The master can estimate $F(\cdot)$ by learning from his collaboration history or making a customer survey. A user can estimate $F(\cdot)$ by checking his or other users' collaboration experiences. There are many public sources (e.g., the master's or some third party's market or customer surveys) that help a user's cost estimation [6], [15].

10. It is sometimes difficult for a user to know his precise loss of privacy before an actual security threat happens to him. Users may face many possible security threats by losing sensitive information, e.g., direct property loss or advertising harassment.

2.3.1 Analysis of Stage II

It turns out that there are multiple equilibria of the collaboration game in Stage II as follows.

Theorem 2 (Stage II Under Symmetrically Incomplete Information). *Stage II admits the following Nash equilibria:*

- (No collaboration): If $R < n_0\mu$, no user will collaborate at any equilibrium in Stage II.
- (Pure strategy NE): If $n_0\mu \leq R < N\mu$ (where $N\mu$ is the product of user number N and the mean μ of user cost distribution), $n^* = \lfloor \frac{R}{\mu} \rfloor$ users choose to collaborate and the remaining users decline. A subset of n^* -out-of- N users is randomly picked up among $\binom{N}{n^*}$ possible subsets. Thus there exist multiple pure NEs in this case.¹¹ If $R \geq N\mu$, all N users will collaborate.
- (Mixed strategy NE): If $n_0\mu < R < N\mu$, every user collaborates with a probability p^* , which is the unique solution to

$$\mathbb{E}_m \left(\left(\frac{R}{m+1} - \mu \right) \mathbf{1}_{\{m+1 \geq n_0\}} \right) = 0, \quad (3)$$

where the expectation \mathbb{E} is taken over the random variable m which follows a binomial distribution $B(N-1, p)$.

The proof of no collaboration and pure strategy NE are given in Appendix B, available in the online supplemental material.

We note that the pure and mixed strategy equilibria in Theorem 2 share a common parameter range, $n_0\mu < R < N\mu$. It should also be noted that the master is not interested in selecting a certain NE since all NEs give him the same performance. Furthermore, Theorem 3 will show that the master will not encourage any mixed NE at the first place.

Next we show how the *mixed strategy NE* p^* is derived. As all users have the same statistical information, we will focus on the symmetric mixed Nash equilibrium. Assume that all users collaborate with a probability p . Consider that there are m users (other than i) who collaborate. If user i collaborates, his expected payoff is

$$u(R, p) := \mathbb{E}_m \left(\left(\frac{R}{m+1} - \mu \right) \mathbf{1}_{\{m+1 \geq n_0\}} \right),$$

where the expectation is taken over m which follows a binomial distribution $B(N-1, p)$, and is independent of user i 's decision.

Given all the other $N-1$ users collaborate with the equilibrium probability p^* , user i 's payoffs by choosing to collaborate or not are the same. Thus p^* should satisfy

$$u(R, p^*) = 0,$$

and is a function of R . Thus we can rewrite p^* as $p^*(R)$. One can show that there exists a mixed strategy Nash equilibrium $p^*(R) \in (0, 1)$ as long as $n_0\mu < R < N\mu$. Note that $R \leq n_0\mu$ leads to $p^*(R) = 0$, which is not a mixed strategy. Also, $R \geq N\mu$ leads to $p^*(R) = 1$, which is not a mixed strategy either.

11. How to select one NE is out of the scope of this paper, and can be referred to [32]. Yet it should be noted that all pure strategy Nash equilibria lead to the same performance for the master as shown in Theorem 3 later on.

2.3.2 Analysis of Stage I

First we consider the case where users use the mixed strategy in Theorem 2 and collaborate with probability $p^*(R)$. The master's expected profit is then

$$f(R) := \mathbb{E}_n ((V - R) \mathbf{1}_{\{n \geq n_0\}}),$$

where the expectation is taken over n which follows a binomial distribution $(N, p^*(R))$. One can show that $f(R)$ has a unique maximum $f(R^*)$, which is positive when $V > n_0\mu$. However, under $n_0\mu < R < N\mu$ there is always a chance that there are less than n_0 users choosing to collaborate under the mixed strategy. Thus the master may want to avoid this. Theorem 2 shows that by choosing $R = n_0\mu$, the master can guarantee n_0 collaborators with a pure strategy Nash equilibrium in Stage II. Any reward value lower than $n_0\mu$ leads to no collaboration, and any value larger than $n_0\mu$ involves a number of collaborators that is larger than necessary (in a pure strategy NE) or does not guarantee enough collaborators (in a mixed strategy NE). As the master's payoff decreases in reward given enough collaborators, we have the following result.

Theorem 3 (Stage I Under Symmetrically Incomplete Information). *The collaboration game admits the following unique SPE:*

- If $V < n_0\mu$, the master will not initiate the collaboration and will choose $R^* = 0$.
- If $V \geq n_0\mu$, the master will announce a reward $R^* = n_0\mu$. A set of n_0 users will collaborate in Stage II. The collaborators achieve a zero expected payoff, and the master achieves a profit $V - n_0\mu$.

2.4 Collaboration under Asymmetrically Incomplete Information

In this section, we study the case where each user i knows his own exact cost C_i , but not other users' costs. The master only knows $F(\cdot)$.¹²

2.4.1 Analysis of Stage II

We have the following result for Stage II.

Theorem 4 (Stage II Under Asymmetrically Incomplete Information). *A user i will collaborate if and only if $C_i \leq \gamma^*(R)$. The common equilibrium decision threshold $\gamma^*(R)$ is the unique solution of $\Phi(\gamma) = 0$, where*

$$\Phi(\gamma) := \mathbb{E}_m \left(\left(\frac{R}{m+1} - \gamma \right) \mathbf{1}_{\{m+1 \geq n_0\}} \right), \quad (4)$$

and the expectation is taken over m which follows a binomial distribution $B(N-1, F(\gamma))$. The equilibrium $\gamma^*(R)$ satisfies $\frac{R}{N} < \gamma^*(R) < \frac{R}{n_0}$.¹³

As (4) is independent of C_i when each user i makes his decision, all users have the same decision threshold. The intuition is that each user has the same information and estimation about others. But different users would still make

12. This is possible when users already learn about their private costs over time, yet the master may not be able to track and collect these sensitive information.

13. We can also show that a user will not be better off by changing from the current pure strategy to any mixed strategy.

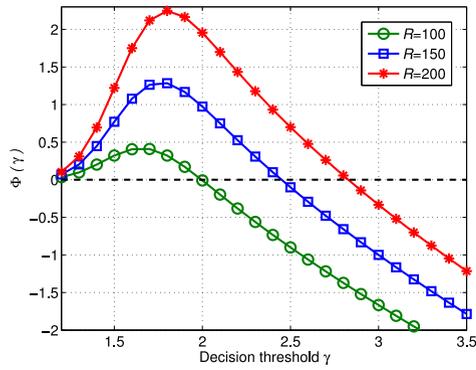


Fig. 2. $\Phi(\gamma)$ as a function of γ and R . Other parameters are $n_0 = 40$ and $N = 100$. We consider a uniform cost distribution with $F(\gamma) = \min(\gamma/4, 1)$. The threshold values $\gamma^*(R)$ for the three different values of R (in ascending order) values are 2.0, 2.4, and 2.8, respectively.

different decisions as their private information about their own collaboration costs are different.

To see why Stage II has the pure NE in Theorem 4, we consider that all users other than i collaborate if and only if their costs are less than some threshold $\gamma > 0$. If user i collaborates, his payoff is

$$\left(\frac{R}{m+1} - C_i\right) \mathbf{1}_{\{m+1 \geq n_0\}},$$

where m follows a binomial distribution $B(N-1, F(\gamma))$ and represents the number of users (other than i) who collaborate. (Recall that cdf $F(\gamma) = P(C_i \leq \gamma)$.) Accordingly, the expected payoff of user i if he collaborates is

$$\mathbb{E}_m \left(\left(\frac{R}{m+1} - C_i \right) \mathbf{1}_{\{m+1 \geq n_0\}} \right), \quad (5)$$

and zero otherwise. At the Nash equilibrium, (5) should equal to 0 when $C_i = \gamma$. That is, having the common collaboration threshold γ is a Nash equilibrium if and only if $\Phi(\gamma) = 0$. We denote the solution to $\Phi(\gamma) = 0$ in (4) as $\gamma^*(R)$. In Appendix C, available in the online supplemental material, we prove that there always exists a unique $\gamma^*(R)$, which satisfies $\frac{R}{N} < \gamma^*(R) < \frac{R}{n_0}$.

Fig. 2 shows $\Phi(\gamma)$ as a function of both γ and R . The solution $\gamma^*(R)$ to $\Phi(\gamma) = 0$ is always unique and satisfies $\frac{R}{N} < \gamma^*(R) < \frac{R}{n_0}$. When $R = 100$, for example, we have $\gamma^*(R) = 2$, which is larger than $R/N = 1$ and is smaller than $R/n_0 = 2.5$. It is also interesting to notice that all users share the same decision threshold $\gamma^*(R)$ although they have different costs.

Theorem 5. *The equilibrium decision threshold $\gamma^*(R)$ increases in R , and decreases in N and n_0 .*

The proof of Theorem 5 is given in Appendix D, available in the online supplemental material.

As N or n_0 increases, more users need to participate in the collaboration and thus the shared reward per collaborator decreases. Therefore, the decision threshold decreases and each user is less likely to collaborate.

2.4.2 Analysis of Stage I

We are now ready to consider Stage I. Given users' equilibrium strategies based on threshold $\gamma^*(R)$ in Stage II in

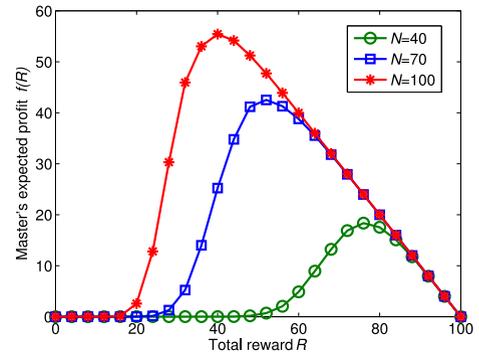


Fig. 3. Master's expected profit $f(R)$ as a function of R and N . Other parameters are $n_0 = 30$ and $V = 100$. Also, we consider a uniform cost distribution with $F(\gamma) = \min(\gamma/3, 1)$. The optimal reward values for different N values (in ascending order) are 77, 52, and 40, respectively.

Theorem 4, the master chooses reward R to maximize his expected profit, i.e.,

$$\max_R f(R) = \mathbb{E}_n((V - R) \mathbf{1}_{\{n \geq n_0\}}), \quad (6)$$

where the expectation is taken over n which follows a binomial distribution $B(N, F(\gamma^*(R)))$. A smaller reward R leads to a larger value of $V - R$, but decreases the collaboration success probability $P(n \geq n_0; R)$.

Let us denote the master's equilibrium choice of reward in Stage I as R^* , which is the optimal solution to Problem (6). To solve Problem (6), we can use any one-dimensional exhaustive search algorithm to find the global optimal solution. Next we verify that the computation complexity is not high. We can approximate the continuity of the feasible range $[0, V]$ of reward R through a proper discretization, i.e., representing all possibilities of R by \bar{V} equally spaced values (with the first and last values equal to 0 and V , respectively). Since the user decision threshold $\gamma^*(R)$ for each possible value of reward R belongs to the range $[0, V]$ (due to $\gamma^*(R) \leq R$ and $R \leq V$), we can similarly discretize this continuous range of $\gamma^*(R)$ by \bar{V} possible values. To derive $\gamma^*(R)$ for each possible R value, we need to search over all \bar{V} possibilities of $\gamma^*(R)$ to approximately solve $\Phi = 0$ in (4), and to derive the optimal R^* we need to further search over all \bar{V} possibilities of R , and thus the overall computation complexity to solve Problem (6) is $\mathcal{O}(\bar{V}^2)$. The choice of \bar{V} depends on the master's tolerance level of the quantization error, and a larger \bar{V} value leads to a more accurate solution with more computation overhead.

Theorem 6. *The equilibrium expected profit $f(R^*)$ of the master increases in V and N , and decreases in n_0 .*

The proof of Theorem 6 is given in Appendix E, available in the online supplemental material. Similarly, we can show that the optimal reward R^* increases in V and n_0 , and decreases in N .

As the master's revenue V increases, he benefits more from the collaboration. As the threshold n_0 increases, however, each user is less likely to collaborate. Thus the master has to give a larger total reward to attract enough collaborators. This decreases his expected profit.

Fig. 3 shows that the master's expected profit $f(R)$ as a function of R and N . We can see that both $f(R)$ and the equilibrium $f(R^*) = \max_R f(R)$ are increasing in N . Intuitively,

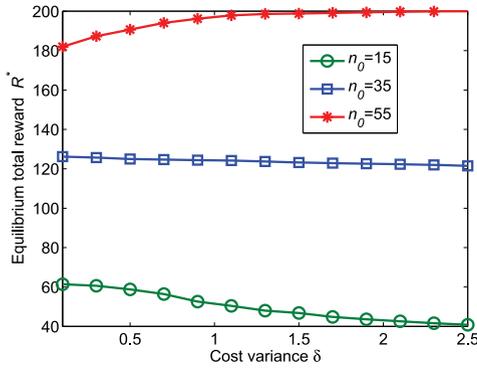


Fig. 4. Master's equilibrium reward R^* as a function of variance δ and n_0 . Other parameters are $N = 80$, $V = 210$, and $\mu = 3$.

as N increases, more users have small collaboration costs (as the cdf function $F(\cdot)$ does not change), and more users will collaborate under the same total reward. Thus the master can lower the equilibrium reward R^* and obtain a larger expected profit.

Next we study how the master's equilibrium total reward and expected profit change with the cdf function $F(\cdot)$ of a user's collaboration cost. We pick Gaussian distribution for example, which can be explicitly characterized by mean μ and variance δ only. This is the case where the master aggregates his cost observations over a large number of user samples.¹⁴

Observation 1. The master's equilibrium total reward R^* increases in mean μ (and his expected profit decreases in μ). Moreover, the optimal reward R^* increases in variance δ for large n_0 and decreases in δ for small n_0 .

The relationship between R^* and μ is quite intuitive, as the master needs to decide a larger R^* to compensate each collaborator's increased cost in expected sense. We next elaborate the impact of δ on R^* .

Fig. 4 shows R^* as a function of variance δ and n_0 , where the master with smaller n_0 requirement can efficiently build the database with smaller reward R^* . When the master requires a large n_0 , he needs to incentivize most users to join the collaboration. As δ increases, some users are more likely to realize much larger costs than μ and the conservative master still needs to incentivize them. Thus R^* increases in δ in this case. When the master only requires a small n_0 , he can target at those users with smallest costs. As δ increases, these users are more likely to have much smaller costs than μ and the master only needs to decide smaller R^* to incentivize them.

We can similarly show in Fig. 5 that as δ increases, the master with large n_0 requirement obtains smaller expected profit $f(R^*)$, whereas the master with small n_0 requirement obtains larger $f(R^*)$. Notice that $f(R^*)$ decreases in requirement n_0 , which is consistent with Theorem 6.

As the users' costs are random variables and have different realizations in different time slots, we explore how the master's equilibrium realized profit changes with time and cost variance δ in the newly added Fig. 6 when the

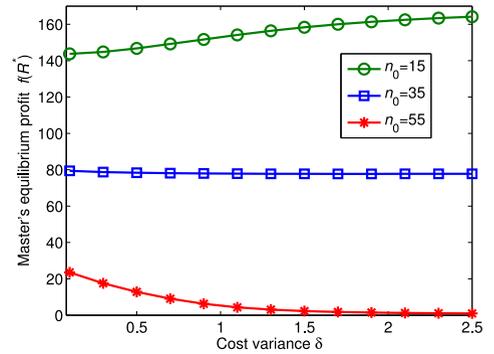


Fig. 5. Master's equilibrium expected profit $f(R^*)$ as a function of variance δ and n_0 . Other parameters are $N = 80$, $V = 210$ and $\mu = 3$.

contributor threshold $n_0 = 55$. Notice that for each δ value, the optimal reward R^* is determined to maximize *expected* profit based on users' cost distributions, and does not depend on the cost realizations in each time slot. The realized profit is either $V - R^*$ or 0, depending on whether the collaboration is successful in that time slot (i.e., $n \geq n_0$) according to (6). As δ increases, the master's realized profit in Fig. 6 decreases most of the time (except time slots 3 and 14). This is consistent with the result in Fig. 5 regarding the equilibrium expected profit when $n_0 = 55$. Furthermore, Fig. 6 shows that a larger variation δ leads to more fluctuations of the master's realized profit. This means that when n_0 is large, the master prefers a smaller cost variation in order to have a larger realized profit in most of the time slots. When n_0 is small (e.g., $n_0 = 15$), we can show that (through a figure of a similar style as Fig. 6) that the master prefers a larger cost variation instead. We do not include the small n_0 case here due to the space limit.

By comparing the performances of the master and users under complete information, symmetrically incomplete information, and asymmetrically incomplete information, we have the following result.

Theorem 7. At the equilibrium of the collaboration game, the master obtains the smallest expected profit under asymmetrically incomplete information, whereas the users obtain the smallest (zero) expected payoffs under symmetrically incomplete information.

Theorem 7 shows that the users benefit from knowing their own costs, while the master incurs profit loss when the

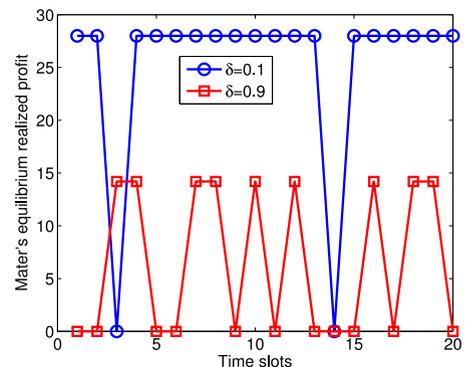


Fig. 6. Master's equilibrium realized profit in time horizon. Other parameters are $N = 80$, $V = 210$, $n_0 = 55$ and $\mu = 3$.

14. Note that the following results also apply to uniform distribution, and we skip the discussion here due to the page limit.

users know their costs and can hide the information from the master.

Recall that the master obtains an expected profit $V - n_0\mu$ under symmetrically incomplete information, and obtains a profit $V - n_0C_0$ under complete information. The relation between these two values depends on N , n_0 , and $F(\cdot)$. Take the uniform distribution $F(\cdot)$ as an example. If n_0 is much smaller than $N/2$, the expected value of C_0 will be smaller than μ and the master is better off under complete information.

3 COLLABORATIONS ON DISTRIBUTED COMPUTING

3.1 System Model on Distributed Computation

In this type of applications, the master solicits the collaboration of smartphone users to perform distributed computing.¹⁵ Different from requiring fixed and periodic data reporting as in data acquisition applications, the master here can assign different amounts of work to different user types. Smartphones are generally different in terms of CPU performance, memory and storage, battery life, and connectivity [17]. Even with the same smartphones, two users may have different phone usage behaviors and different sensitivities (e.g., energy consumption).

One can imagine that the energy consumption will hinder the smartphones' involvement in distributed computing, which motivates us to consider smartphones' energy constraints (i.e., battery capacity limits) in the modeling of \bar{t}_i in (8). Meanwhile, we want to highlight that it is already feasible for smartphones to support distributed computing. First, the large number of smartphones can help compensate the energy limitation of each individual phone [11]. Then the energy consumed by an individual smartphone is not large. Second, the energy limitation will be of a less concern for smartphones which have access to charging facilities (as the reviewer has pointed out). With the newly developed wireless charging technologies (e.g., inductive and magnetic resonance couplings), more smartphones can be supported even when they are moving around [33]. Third, the battery technologies and energy management algorithms have been significantly improved during the recently years (e.g., [12], [13]). Finally, today's data storage technologies make it possible to store tens of gigabytes of data in a small memory card, which means that some of today's smartphones are almost as capable as desktop computers from several years back [34].

We consider a total of N users belonging to a set $\mathcal{I} = \{1, \dots, I\}$ of I types. Each type $i \in \mathcal{I}$ has $N_i \geq 1$ users, with $\sum_{i \in \mathcal{I}} N_i = N$. A type- i user can perform at most \bar{t}_i units of work, and faces a cost K_i per unit of work he performs. The upper bound of \bar{t}_i reflects the limited battery capacity, time constraint, or other physical constraints. Users know their unit costs before the collaboration, since (i) many factors of these costs (e.g., power consumption) are explicitly reflected by smartphones' technical specifications, and (ii) users explicitly know their own sensitivities (e.g., to power

consumption) in costs. Note that the data exchanged between users and the master are not sensitive to users. This is different from data acquisition, where costs also come from implicit insecurity. To determine the unit cost values, one can check [28] and [29] for energy consumption data (e.g., radio power in joule per minute) in specific applications.

The payoff of a type- i user who accomplishes t units of work and receives a reward r from the master is

$$u_i(r, t) = r - K_i t, \text{ for } 0 \leq t \leq \bar{t}_i. \quad (7)$$

Note that the user can always choose not to collaborate with the master and thus receive zero payoff with $t = r = 0$.¹⁶ Without loss of generality, we order user types in the descending order of the *unit cost*, i.e., $K_1 > K_2 > \dots > K_I$, i.e., a higher type of user has a smaller cost. Note that if any two types have the same unit cost, we can group them together as a single type. It should also be mentioned that this unit-cost ordering is different from the way that we order smartphone users' *constant* collaboration costs in Section 2.

By asking each type- i user to accomplish the amount t_i of work and rewarding him with r_i , the master's profit is¹⁷

$$\pi(\{(r_i, t_i)\}_{i \in \mathcal{I}}) = \sum_{i \in \mathcal{I}} (\theta_i \log(1 + N_i t_i) - N_i r_i). \quad (8)$$

The term $\theta_i \log(1 + N_i t_i)$ is increasing in users' efforts and well characterizes the master's diminishing return (or utility) from the total work $N_i t_i$ finished by type- i (as in [35], [36]).¹⁸ The parameter $\theta_i > 0$ characterizes the master's preference for work performed by type- i users, and does not depend on K_i .¹⁹ Notice that we do not require θ_i 's to be monotonically ordered. The term $N_i r_i$ in (8) is the total reward that the master offers to type- i users. The summation operation in (8) is motivated by the fact that many complex engineering or commercial problems can be separated into multiple subproblems and solved in a distributed manner (e.g., [13], [19]).

By examining (7) and (8), we can see that the master and users have conflicting objectives. The master wants users to accomplish a larger task, which increases the master's utility as well as users' collaboration costs. Users want to obtain a larger reward, which decreases the master's profit. Next we study how master and users interact through a contract.

16. Note that rewards and tasks are related in a properly designed contract, and one would expect that the reward increases with the corresponding task amount. We will analytically characterize such a relationship later on.

17. Here the summation operation is taken outside the logarithmic terms, as it is hard to coordinate different user types (in operation systems, computing speeds, and storage capabilities) in the same computing task due to compatibility and synchronization issues and they will be responsible for different tasks at the same time.

18. The assumed logarithmic utility term helps us derive closed-form solutions and engineering insights. Using other concave terms with diminished return are not likely to change the main conclusions.

19. The value of θ_i depends on how easily the master can combine the computing efforts of this type with other types' efforts to finalize the computing result. Notice that θ_i is large if the master's communication with type- i users is efficient (e.g., with small delay) or the type- i 's operation system becomes highly compatible with the master's system to handle computing tasks.

15. PCs are also suitable to handle distributed computing given a lot more power. Our results here can also be applicable for those PCs which are underutilized and can connect to Internet for networking.

3.2 Master-Users Contractual Interactions

Contract theory studies how an economic decision-maker constructs contractual arrangements, especially in the presence of asymmetric (private) information [23]. In our case, the user types are private information.

The master proposes a contract that specifies the relationship between a user's amount of task t and reward r . Specifically, a *contract* is a set $\mathcal{C} = \{(t_1, r_1), \dots, (t_M, r_M)\}$ of $M \geq 1$ (amount of task, reward)-pairs that are called *contract items*. The master proposes \mathcal{C} . Each user selects a contract item (t_m, r_m) and performs the amount of work t_m for the reward r_m . According to [23], it is optimal for the master to design a contract item for each type, i.e., $M = I$. Note that a user can always choose not to work for the master, which implies an implicit contract item $(r, t) = (0, 0)$ (often not counted in the total number of contract items). Once a user accepts some contract item, he needs to accomplish the task and the master needs to reward him according to that item.

Each type of users selects the contract item that maximizes his payoff in (7). The master wants to optimize the contract items and maximize his profit in (8). We will again focus on a two-stage Stackelberg game, where the master proposes the contract first and users choose the contract items afterwards.

Next, we study how the master determines the contract that maximizes his profit, depending on what information he has about the users' types. As explained in the beginning of Section 3.1, we assume that a user knows his unit cost. This means that we only need to consider two information scenarios, complete information and asymmetrically incomplete information, depending on what the master knows.

3.3 Contract Design under Complete Information

In this section, we study the case where the master knows the type of each user though this case is not easy to realize in practice. The analysis of this section mainly serves as a benchmark for understanding the more realistic incomplete information scenario in next section. Under complete information, it is feasible for the master to monitor and make sure that each type of users accepts only the contract item designed for that type. The master needs to ensure that each user has a non-negative payoff so that the user will accept the contract. In other words, the contract should satisfy the following individual rationality constraints.

Definition 1 (IR: Individual rationality). *A contract satisfies the individual rationality constraints if each type- i user receives a non-negative payoff by accepting the contract item for type- i , i.e.,²⁰*

$$r_i - K_i t_i \geq 0, \quad \forall i \in \mathcal{I}. \quad (9)$$

Under complete information, the optimal contract $\mathcal{C} = \{(r_i^*, t_i^*)\}_{i \in \mathcal{I}}$ solves the following problem:

20. We can easily extend our model by considering a reservation payoff $u_0 > 0$ for all users, which represents their benefit by making an alternative choice besides joining in the collaboration. By following a similar analysis, we can still show that the new IR constraints $r_i - K_i t_i \geq u_0$ are tight at the contract optimality for any type- i user who joins in the collaboration. The key difference is that the master now needs to match users' reservation payoffs by announcing larger rewards, which is slightly different from Theorem 8.

$$\begin{aligned} \max_{\{(r_i, t_i)\}_{i \in \mathcal{I}}} \quad & \pi(\{(r_i, t_i)\}_{i \in \mathcal{I}}) = \sum_{i \in \mathcal{I}} (\theta_i \log(1 + N_i t_i) - N_i r_i), \\ \text{subject to:} \quad & \text{IR constraints (9) and } 0 \leq t_i \leq \bar{t}_i, \forall i \in \mathcal{I}. \end{aligned} \quad (10)$$

It is easy to check that the IR constraints are tight at the optimal solution to Problem (10), and the master will leave a zero payoff to each type- i user with $r_i^* = K_i t_i^*$. Also, due to the independence of each type in Problem (10), we can decompose Problem (10) into I subproblems. For each type $i \in \mathcal{I}$, the master needs to solve the following subproblem:

$$\begin{aligned} \max_{t_i} \quad & \pi_i(t_i) = \theta_i \log(1 + N_i t_i) - N_i K_i t_i, \\ \text{subject to:} \quad & 0 \leq t_i \leq \bar{t}_i. \end{aligned} \quad (11)$$

By solving all I subproblems, we have the following result.

Theorem 8 (Optimal Contract Under Complete Information). *At the equilibrium, the master will hire the type- i users if and only if $\theta_i > K_i$. The total involved user type set is*

$$\mathcal{I}_C = \{i \in \mathcal{I} : \theta_i > K_i\}. \quad (12)$$

The subscript C in \mathcal{I}_C refers to the complete information assumption. For a user with type $i \in \mathcal{I}_C$, the equilibrium contract item is

$$\begin{aligned} (r_i^*, t_i^*) &= (K_i t_i^*, t_i^*) \\ &= \left(\min\left(\frac{\theta_i - K_i}{N_i}, K_i \bar{t}_i\right), \min\left(\frac{\theta_i - K_i}{K_i N_i}, \bar{t}_i\right) \right). \end{aligned} \quad (13)$$

For a user with type $i \notin \mathcal{I}_C$, the equilibrium contract item is $(r_i^, t_i^*) = (0, 0)$. All users (no matter joining collaboration or not) receive a zero payoff. The master's equilibrium profit is*

$$\begin{aligned} \pi^* &= \sum_{i \in \mathcal{I}_C} \\ & \min\left(\theta_i \log\left(\frac{\theta_i}{K_i}\right) - \theta_i + K_i, \theta_i \log(1 + N_i \bar{t}_i) - N_i K_i \bar{t}_i\right). \end{aligned} \quad (14)$$

The proof of Theorem 8 is given in Appendix G, available in the online supplemental material.

Intuitively, the master needs to compensate a collaborator's cost, thus he will hire type- i users only when his preference characteristic θ_i is larger than the unit cost of that type K_i . Users will receive a zero payoff since their private information about unit costs are known to the master.

By looking into all parameters in the equilibrium contract in (13) and payoff π^* in (14), we have the following observation.

Observation 2. For $i \in \mathcal{I}_C$, the equilibrium task t_i^* to a type- i user increases in θ_i , and decreases in N_i and K_i . The master may or may not offer a larger task or reward to a higher type- i collaborator, depending on N_i and θ_i for that type. Also, the master's equilibrium profit π^* increases in θ_i , N_i , and \bar{t}_i , and decreases in K_i .

Notice that a higher type- i collaborator has less unit cost where the master needs to compensate, but the master may

not give him a larger task or reward. This can happen when there are too many collaborators of that type, or the master evaluates this type with a small value of θ_i .

3.4 Master's Contract Design under Asymmetrically Incomplete Information

In this section, we study the case where the master only has asymmetrically incomplete information about each user's type. A user's actual type is only known to himself, and the master and the other users only have a rough estimation on this. We consider that others believe a user belonging to type- i with a probability q_i . Everyone knows the total number of users N .²¹

3.4.1 Feasibility of Contract under Asymmetrically Incomplete Information

According to [23], the master's contract should first be feasible in this scenario. A feasible contract must satisfy both individual rationality constraints (Definition 1 in Section 3.3) and incentive compatibility constraints defined as follows.

Definition 2 (IC: Incentive compatibility). A contract satisfies the incentive compatibility constraints if each type- i user prefers to choose the contract item for his own type, i.e.,

$$r_i - K_i t_i \geq r_j - K_j t_j, \quad \forall i, j \in \mathcal{I}. \quad (15)$$

Under asymmetrically incomplete information, the master does not know the number of users N_i of type- i . Let us denote the users' numbers of all types as $\{n_i\}_{i \in \mathcal{I}}$, which are random variables following certain distributions and satisfying $\sum_{i \in \mathcal{I}} n_i = N$. Note that the realizations of $\{n_i\}_{i \in \mathcal{I}}$ depend on N and probabilities $\{q_i\}_{i \in \mathcal{I}}$ of all types that a user may belong to. The master's profit for a particular realization of $\{n_i\}_{i \in \mathcal{I}}$ is

$$\pi(\{(r_i, t_i)\}_{i \in \mathcal{I}}, \{n_i\}_{i \in \mathcal{I}}) = \sum_{i \in \mathcal{I}} (\theta_i \log(1 + n_i t_i) - n_i r_i). \quad (16)$$

Thus the master's expected profit is

$$\begin{aligned} & \mathbb{E}_{\{n_i\}_{i \in \mathcal{I}}} [\pi(\{(r_i, t_i)\}_{i \in \mathcal{I}}, \{n_i\}_{i \in \mathcal{I}})] \\ &= \sum_{n_1=0}^N \sum_{n_2=0}^{N-n_1} \cdots \sum_{n_{I-1}=0}^{N-\sum_{j=1}^{I-2} n_j} \frac{N! q_1^{n_1} \cdots q_{I-1}^{n_{I-1}} q_I^{N-\sum_{j=1}^{I-1} n_j}}{n_1! \cdots n_{I-1}! (N - \sum_{j=1}^{I-1} n_j)!} \\ & \quad \cdot \pi(\{(r_i, t_i)\}_{i \in \mathcal{I}}, \{n_i\}_{i \in \mathcal{I}}). \end{aligned} \quad (17)$$

The master's profit optimization problem as²²

$$\begin{aligned} & \max_{\{(r_i, t_i)\}_{i \in \mathcal{I}}} \mathbb{E}_{\{n_i\}_{i \in \mathcal{I}}} [\pi(\{(r_i, t_i)\}_{i \in \mathcal{I}}, \{n_i\}_{i \in \mathcal{I}})] \\ & \text{subject to: IR constraints in (9),} \\ & \quad \text{IC constraints in (15),} \\ & \quad 0 \leq t_i \leq \bar{t}_i, \forall i \in \mathcal{I}. \end{aligned} \quad (18)$$

21. Users can know N by checking the master's or some third party's market survey, or the news on recent penetration or shipment of smartphones.

22. After observing all I reward-task combinations in $\{(r_i, t_i)\}_{i \in \mathcal{I}}$, it is optimal for any type- i user to choose only (r_i, t_i) of his own type later, according to IR and IC constraints in the contract mechanism.

The total number of IR and IC constraints is I^2 . Next, we show that it is possible to represent these I^2 constraints with a set of much fewer equivalent constraints.

Proposition 1. (Sufficient and Necessary Conditions for Feasibility). For a contract $\mathcal{C} = \{(r_i, t_i), \forall i \in \mathcal{I}\}$ with user costs $K_1 > \cdots > K_I$, it is feasible if and only if all the following conditions are satisfied:

- 1) Condition(+): $r_1 - K_1 t_1 \geq 0$;
- 2) Condition(\uparrow):
 $0 \leq r_1 \leq \cdots \leq r_I$ and $0 \leq t_1 \leq \cdots \leq t_K$;
- 3) Condition(\leq): For any $i = 2, \dots, I$,

$$r_{i-1} + K_i(t_i - t_{i-1}) \leq r_i \leq r_{i-1} + K_{i-1}(t_i - t_{i-1}). \quad (19)$$

The proof of Proposition 1 is given in Appendix H, available in the online supplemental material.

Intuitively, Condition(+) ensures that all types of users can get a nonnegative payoff by accepting the contract item (r_1, t_1) , as it implies $r_1 - K_j t_j \geq 0$ for all $j \geq 2$. Thus this can replace the IR constraints in (9). Condition(\uparrow) and Condition(\leq) are related to IC constraints in (15). Condition(\uparrow) shows that a user with a higher type should be assigned a larger task, because his unit cost is lower (and more efficient) and the master needs to compensate this user less per unit work. Also, a larger reward should be given to this user for the larger task undertaken by him, otherwise this user will choose another contract item in order to work less. Condition(\leq) shows the relation between any two neighboring contract items.

Based on Proposition 1, we can simplify the master's problem in (18) as

$$\begin{aligned} & \max_{\{(r_i, t_i)\}_{i \in \mathcal{I}}} \mathbb{E}_{\{n_i\}_{i \in \mathcal{I}}} [\pi(\{(r_i, t_i)\}_{i \in \mathcal{I}}, \{n_i\}_{i \in \mathcal{I}})] \\ & \text{subject to, Condition(+), Condition(\uparrow), Condition(\leq),} \\ & \quad 0 \leq t_i \leq \bar{t}_i, \forall i \in \mathcal{I}, \end{aligned} \quad (20)$$

where the previous I^2 IR and IC constraints have been reduced to $I + 2$ constraints.

3.4.2 Analysis by Sequential Optimization

Now we want to solve the master's optimal contract. However, (20) is not easy to solve as it has coupled variables and many constraints. The way we solve is a sequential optimization approach: we first derive the optimal rewards $\{r_i^*(\{t_i\}_{i \in \mathcal{I}})\}_{i \in \mathcal{I}}$ given any feasible tasks $\{t_i\}_{i \in \mathcal{I}}$, then further derive the optimal tasks $\{t_i^*\}_{i \in \mathcal{I}}$ for the optimal contract.

Proposition 2. Let $\mathcal{C} = \{(r_i, t_i)\}_{i \in \mathcal{I}}$ be a feasible contract with any feasible tasks $0 \leq t_1 \leq \cdots \leq t_I$. The unique optimal rewards $\{r_i^*(\{t_i\}_{i \in \mathcal{I}})\}_{i \in \mathcal{I}}$ satisfy

$$r_1^*(\{t_i\}_{i \in \mathcal{I}}) = K_1 t_1, \quad (21)$$

$$\begin{aligned} r_i^*(\{t_i\}_{i \in \mathcal{I}}) &= r_{i-1}^* + K_i(t_i - t_{i-1}) \\ &= K_1 t_1 + \sum_{j=2}^i K_j(t_j - t_{j-1}), \forall i = 2, \dots, I. \end{aligned} \quad (22)$$

Notice that the lowest type user obtains a zero payoff, and a user's optimal payoff is non-decreasing in his type.

Proof (Sketch). First, we can prove (21) by showing that Condition(+) binds at the optimality. This guarantees the IR constraints of the contract. Second, we can prove (22) by showing that the left-hand side inequality in Condition(\leq) binds at the optimality. This guarantees the IC constraints of the contract. Finally, (21) shows a zero payoff for the lowest type user, and (22) shows that for any $\{t_i\}_{i=1}^I$,

$$r_i^* - K_i t_i = r_{i-1}^* - K_i t_{i-1},$$

which is no smaller than $r_{i-1}^* - K_{i-1} t_{i-1}$ due to $K_i < K_{i-1}$. Thus a user's payoff is non-decreasing in his type. \square

Based on Proposition 2, we can greatly simplify the master's optimization Problem in (20) as

$$\begin{aligned} & \max_{\{t_i\}_{i \in \mathcal{I}}} \mathbb{E}_{\{n_i\}_{i \in \mathcal{I}}} [\pi(\{(r_i^*(\{t_i\}_{i \in \mathcal{I}}), t_i)\}, \{n_i\}_{i \in \mathcal{I}})] \\ & \text{subject to, } 0 \leq t_1 \leq \dots \leq t_I, \\ & t_i \leq \bar{t}_i, \forall i \in \mathcal{I}. \end{aligned} \quad (23)$$

Next we first examine whether Problem (23) is a convex problem and then derive a way to solve it. The first derivative of the master's expected profit over t_i is

$$\begin{aligned} & \frac{\partial \mathbb{E}_{\{n_i\}_{i \in \mathcal{I}}} [\pi(\{(r_i^*(\{t_i\}_{i \in \mathcal{I}}), t_i)\}, \{n_i\}_{i \in \mathcal{I}})]}{\partial t_i} \\ & = \sum_{n_1=0}^N \sum_{n_2=0}^{N-n_1} \dots \sum_{n_{I-1}=0}^{N-\sum_{j=1}^{I-2} n_j} \frac{N! q_1^{n_1} \dots q_{I-1}^{n_{I-1}} q_I^{N-\sum_{j=1}^{I-1} n_j}}{n_1! \dots n_{I-1}! (N - \sum_{j=1}^{I-1} n_j)!} \\ & \quad \left(\frac{n_i \theta_i}{1 + n_i t_i} - n_i K_i - (K_i - K_{i+1}) \sum_{\forall j > i, \forall j \in \mathcal{I}} n_j \right), \forall i \in \mathcal{I}, \end{aligned} \quad (24)$$

which is independent of t_j for any $j \neq i$. From (24), we can easily check the Hessian matrix of the objective function in Problem (23) and conclude that it is concave in $\{t_i, i \in \mathcal{I}\}$. Furthermore, the constraints in Problem (23) are all linear and the feasible set in Problem (23) is convex and not empty. Thus we conclude that Problem (23) is convex. It should be noted that the feasible set of Problem (23) has interior such that the strict inequalities hold for all constraints in Problem (23). For example, for any positive value η , such an interior point feasible for Problem (23) could be

$$t_i = \frac{\min(\{\bar{t}_i, \forall i \in \mathcal{I}\})}{I - i + 1 + \eta}, \forall i \in \mathcal{I}.$$

Thus Problem (23) is a convex problem satisfying Slater's condition (implying strong duality) and always has a solution, and can be optimally solved by examining KKT conditions.

The Lagrangian function is

$$\begin{aligned} & L(\{t_i, i \in \mathcal{I}\}, \{\lambda_i, i \in \mathcal{I} \setminus \{I\}\}, \{v_i, i \in \mathcal{I}\}) \\ & = \mathbb{E}_{\{n_i\}_{i \in \mathcal{I}}} [\pi(\{(r_i^*(\{t_i\}_{i \in \mathcal{I}}), t_i)\}, \{n_i\}_{i \in \mathcal{I}})] + \sum_{i \in \mathcal{I}} v_i (\bar{t}_i - t_i) \\ & \quad + \sum_{i \in \mathcal{I} \setminus \{I\}} \lambda_i (t_{i+1} - t_i), \end{aligned} \quad (25)$$

where $\{\lambda_i, i \in \mathcal{I} \setminus \{I\}\}$ and $\{v_i, i \in \mathcal{I}\}$ are Lagrange multipliers corresponding to the constraints in Problem (23). The KKT conditions are as follows:

- *Primal constraints:* $t_i^* \leq t_{i+1}^*, \forall i \in \mathcal{I} \setminus \{I\}; t_i^* \leq \bar{t}_i, \forall i \in \mathcal{I};$
- *Dual constraints:* $\lambda_i^* \geq 0, \forall i \in \mathcal{I} \setminus \{I\},$ and $v_i^* \geq 0, \forall i \in \mathcal{I};$
- *Complementary slackness:* $\lambda_i^* (t_{i+1}^* - t_i^*) = 0, \forall i \in \mathcal{I} \setminus \{I\},$ and $v_i^* (\bar{t}_i - t_i^*) = 0, \forall i \in \mathcal{I};$
- *First-order condition of Lagrangian with respect to t_i :*

$$\begin{aligned} \partial L / \partial t_1 &= \partial \mathbb{E}_{\{n_i\}_{i \in \mathcal{I}}} [\pi(\{(r_i^*(\{t_i\}_{i \in \mathcal{I}}), t_i)\}, \{n_i\}_{i \in \mathcal{I}})] / \partial t_1 \\ & \quad - \lambda_1 - v_1 = 0, \\ \partial L / \partial t_i &= \partial \mathbb{E}_{\{n_i\}_{i \in \mathcal{I}}} [\pi(\{(r_i^*(\{t_i\}_{i \in \mathcal{I}}), t_i)\}, \{n_i\}_{i \in \mathcal{I}})] / \partial t_i \\ & \quad - (\lambda_i - \lambda_{i-1}) - v_i = 0, \forall i \in \mathcal{I} \setminus \{1, I\}, \\ \partial L / \partial t_I &= \partial \mathbb{E}_{\{n_i\}_{i \in \mathcal{I}}} [\pi(\{(r_i^*(\{t_i\}_{i \in \mathcal{I}}), t_i)\}, \{n_i\}_{i \in \mathcal{I}})] / \partial t_I \\ & \quad + \lambda_{I-1} - v_I = 0, \end{aligned} \quad (26)$$

from which we cannot derive closed-form solutions but can rely on numerical methods (e.g., primal dual algorithm) to show numerical results later on.²³ The computation complexity to solve Problem (23) is not high and the complexity upperbound can be derived in the following way. Due to the task relationships among different user types (i.e., $t_1 \leq \dots \leq t_I$ and $t_I \leq \bar{t}_I$), the possible range of each task t_i is $[0, \bar{t}_I]$. We can approximate the continuity of this range through a proper discretization, i.e., representing all possibilities of any t_i by T equally spaced values (with the first and last values equal to 0 and \bar{t}_I , respectively). By (approximately) solving all the KKT conditions especially (26) above, we require computation in order $\mathcal{O}(T)$ to search over all T possibilities for each optimal t_i^* for type- i . The overall computation complexity for all I types is $\mathcal{O}(I \cdot T)$ in Problem (23). The choice of T will affect the quantization error of the computation.

Actually, without explicitly solving Problem (23), we can still derive some interesting results by looking into the KKT conditions as follows.

Theorem 9. *The total involved user type set under asymmetrically incomplete information is*

$$\begin{aligned} \mathcal{I}_A &= \left\{ i \in \mathcal{I} : \right. \\ & \quad \left. \mathbb{E}_{\{n_i\}_{i \in \mathcal{I}}} \left[n_i (\theta_i - K_i) - (K_i - K_{i+1}) \sum_{\forall j > i, j \in \mathcal{I}} n_j \right] > 0 \right\}, \end{aligned} \quad (27)$$

where the subscript A in \mathcal{I}_A refers to the asymmetrically incomplete information assumption.²⁴ Compared with the

23. It should be mentioned that some multiplier λ_i (corresponding to the constraint $t_{i+1} \geq t_i$) may be nonzero when the master has much smaller preference characteristics on higher user type- $(i+1)$ than type- i , or the higher type involves many more users than the lower type. Some multiplier v_i (corresponding to $t_i \leq \bar{t}_i$) may be nonzero when the capacity upper bound \bar{t}_i of type- i is small.

24. Note that the master will design $(r^*, t^*) = (0, 0)$ for the types not in set \mathcal{I}_A . Thus the users of these types are not involved as collaborators.

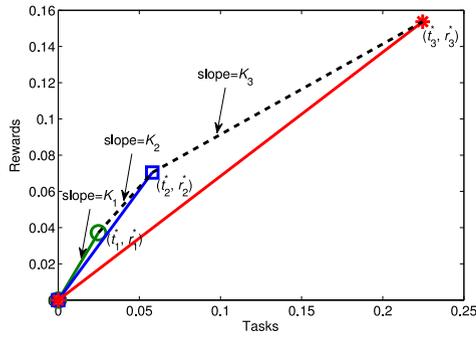


Fig. 7. The master's optimal contract items for three types ($I = 3$). Other parameters are $N = 120$, $K_1 = 1.5$, $K_2 = 1$, $K_3 = 0.5$, $\theta_i = 5$, and $q_i = 1/3$ for any $i \in \mathcal{I}$.

collaborator set \mathcal{I}_C under complete information case, here the master involves less collaborators, i.e., $|\mathcal{I}_A| \leq |\mathcal{I}_C|$. Moreover, the master assigns a larger task and gives a larger reward to a higher type of collaborator, which may not be the case under complete information (see Observation 2). Only the lowest type of collaborator(s) in set \mathcal{I}_A obtains a zero payoff, and higher types of collaborators in set \mathcal{I}_A obtain positive payoffs that are increasing in their types.

The proof of Theorem 9 is given in Appendix I, available in the online supplemental material.

Intuitively, as the master does not know each user's type, he needs to provide incentives (in terms of positive payoffs) to the users to attract them revealing their own types truthfully. If he involves a low type user, he needs to give increasingly higher payoffs to all higher types. Thus he should target at users with high enough types. We have $|\mathcal{I}_A|$ smaller than $|\mathcal{I}_C|$, which means that some low types belong to set \mathcal{I}_C may not be included in set \mathcal{I}_A . By comparing (27) and (12) for the highest type- I , we know that that this type is involved in both information scenarios.

Recall that under complete information, Observation 2 shows that the master may not give a larger task and reward to a higher type- i collaborator. This can happen when θ_i is small or the number of users of that type is large. Under asymmetrically incomplete information, however, the IC constraints require the reward and task to be nondecreasing in the collaborator types, independent of θ_i and the number of users in each type (which is a random variable). Otherwise, some collaborators will have incentives to choose contract items not designed for their own types, and thus violate IC constraints. This is not optimal for the master based on the Revelation Principle [23].

Fig. 7 shows the master's optimal contract $\{(r_i^*, t_i^*)\}_{i=1}^3$ for three collaborator types. A higher type- i user obtains a larger task t_i^* , a larger reward r_i^* , and a larger payoff ($u_i^* = r_i^* - t_i^*$). This is consistent with Proposition 2. The slope of the dashed line between two points (r_i^*, t_i^*) and (r_{i+1}^*, t_{i+1}^*) equals to cost K_{i+1} (as shown in Proposition 2). In the contract, the ratio between the reward and task (i.e., r_i^*/t_i^*) for type- i decreases with the type. Thus a lower type $j < i$ collaborator will not choose the higher contract item (r_i^*, t_i^*) , since it is too costly and not be efficient for him to undertake the task. A user will not choose a lower type contract item either, otherwise his payoff (though still positive) will decrease with a smaller reward.

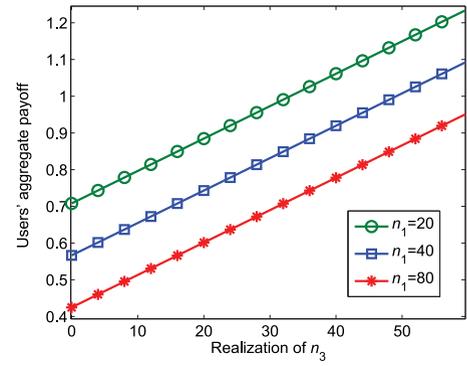


Fig. 8. Users' aggregate payoff under asymmetrically incomplete information as a function of users' realized numbers $\{n_i\}_{i=1}^3$ in three types ($I = 3$). Here we only show n_1 and n_3 , and n_2 can be computed as $N - n_1 - n_3$. Other parameters are $N = 120$, $K_1 = 1.1$, $K_2 = 1$, $K_3 = 0.9$, $\theta_i = 5$, and $q_i = 1/3$ for any $i \in \mathcal{I}$.

By looking into (24), we have the following result.

Observation 3. The master's optimal task allocation t_i^* to a type- i collaborator increases in the master's preference characteristic θ_i and decreases in the collaborator's cost K_i . The master's equilibrium expected profit increases in θ_i for all $i \in \mathcal{I}_A$.

Given the task-reward combinations in the contract, users will benefit from keeping their private information from the master: the lowest type collaborator obtains a zero payoff and a higher type one obtains a larger and positive payoff as in Proposition 2 and Fig. 7. To understand how the hidden information benefits the entire user population, Fig. 8 investigates users' aggregate payoff as we vary the number of users of each of the three types, $\{n_i\}_{i=1}^3$. The total population is fixed at a size of $N = 120$. We can see that the users' aggregate payoff decreases as we have more low type users (n_1), and increases as we have more high type users (n_3). Intuitively, a higher number of type-1 collaborators (n_1) means that more collaborators receive a zero payoff, while a higher number of type-3 collaborators (n_3) means that more collaborators receive the maximum payoff.

It should be noted that the master prefers a large probability of having high type users, as these users are more efficient in performing computing tasks given the same reward. As an example, consider three types of users ($I = 3$): the master enjoys the maximum collaboration benefit when all users belong to the highest type (i.e., $q_1 = q_2 = 0$ and $q_3 = 1$). This is also illustrated in Fig. 7, where the ratio between task and reward (i.e., t_i^*/r_i^*) is the highest for the type-3 users. When all users always belong to the same type, users cannot hide their type information from the master, and the master can hire them by just providing a zero payoff. However, when users have positive probabilities of belonging to different types, they can hide their type information from the master, and the master needs to provide more rewards to motivate high type users to contribute.

Next, we compare the master's profits under complete and asymmetrically incomplete information.

Observation 4. Compared with complete information, the master obtains a smaller equilibrium expected profit

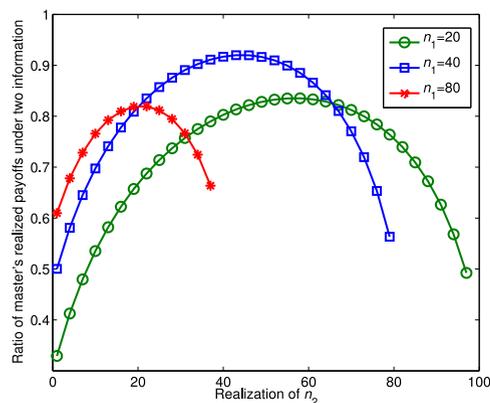


Fig. 9. The ratio of the master's realized payoffs under asymmetrically incomplete and complete information as a function of users' realized numbers $\{n_i\}_{i=1}^3$ in three types ($I=3$). Here we only show n_1 and n_2 , and n_3 equals $N - n_1 - n_2$. Other parameters are $N=120$, $K_1=1.1$, $K_2=1$, $K_3=0.9$, $\theta_i=5$, and $q_i=1/3$ for any $i \in \mathcal{I}$.

under asymmetrically incomplete information. The gap between his realized profit under two information scenarios is minimized when the realization (users' numbers in all types) is the closest to the expected value.

Fig. 9 shows the ratio of the master's realized payoffs under asymmetrically incomplete and complete information, which is a function of users' realizations $\{n_i\}_{i=1}^3$ in all three types. This ratio is no larger than 1, as the master obtains the maximum profit under complete information. This profit ratio reaches its maximum 92 percent when users' type realization matches the expected value, i.e., $n_i = Nq_i = 40$ for $i=1, 2$ (and $n_3 = N - n_1 - n_2 = 40$ as well). This is consistent with the fact that the master maximizes his expected profit under asymmetrically incomplete information. Note that even in this case, there is still a profit loss for the master under asymmetrically incomplete information due to information loss.

4 CONCLUSION

This paper analyzes different mechanisms that a master can use to motivate the collaboration of smartphone users on both *data acquisition* and *distributed computing*. For data acquisition applications, we propose a reward-based collaboration scheme for the master to attract enough users by giving out the minimum reward. For distributed computing applications, we use contract theory to study how a master decides different task-reward combinations for many different types of users.

There are some possible ways to extend the results in this paper. For the data acquisition applications, we can consider a flexible revenue model instead of a threshold one. For example, Google can still benefit if a few users take pictures of some critical events. The master will still give out some reward even facing a small number of users, and his reward and profit would increase as more users choose to collaborate. Moreover, in some network with small number of users, the geographical positions of users could be more important than the total number. We will study such a spatial issue in the future.

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